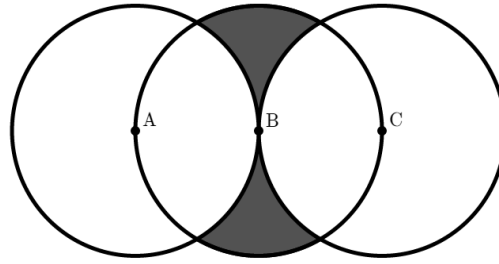
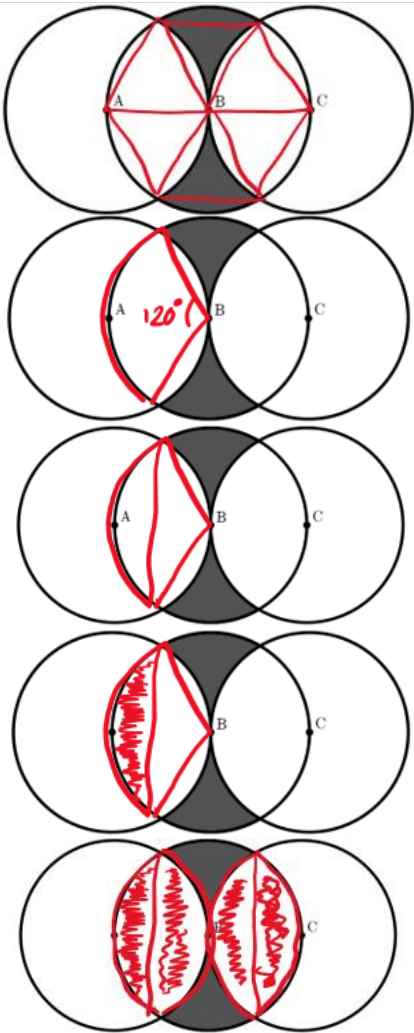


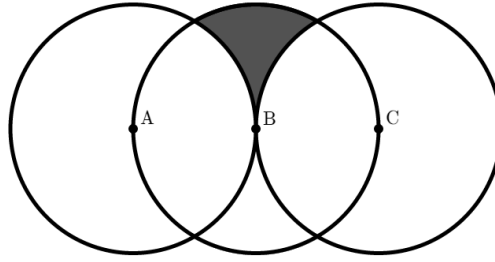
a)  
 The diagram shows three circles, each of radius 4cm.  
 The centres of the circles are A, B and C such that ABC is a straight line and  $AB = BC = 4\text{cm}$ .



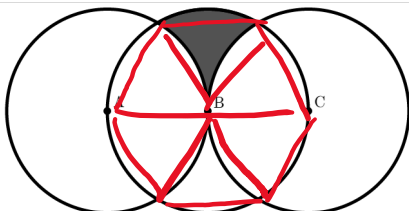
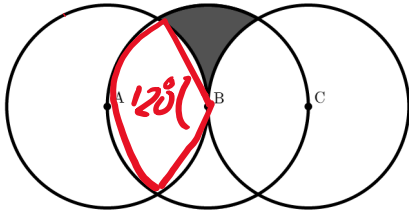
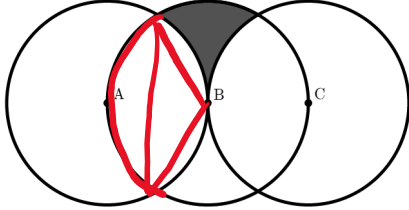
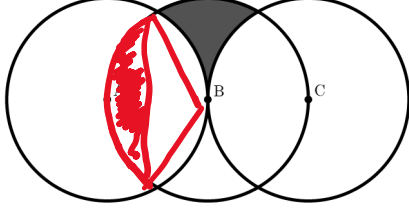
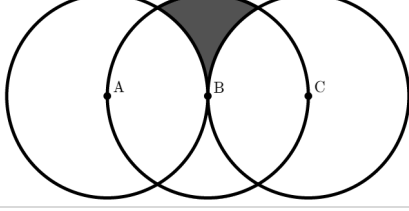
Work out the total area of the two shaded regions.  
 Give your answer in terms of  $\pi$ .

<p>What is the area of each circle?</p>	$A = \pi r^2 = \pi \times 4^2 = 16\pi$
<p>How much of the circle, centre B, is unshaded?</p>	<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <p>A regular hexagon, formed of six equilateral triangles, is inscribed in a circle.</p> <p>Area of the sector = <math>\frac{1}{3} \times 16\pi = \frac{16\pi}{3}</math></p> <p>Area of the triangle = <math>\frac{1}{2} \times 4 \times 4 \times \sin 120 = 8 \times \frac{\sqrt{3}}{2} = 4\sqrt{3}</math></p> <p>Area of the segment = Area of sector - area of triangle = <math>\frac{16\pi}{3} - 4\sqrt{3}</math></p> <p>Red area = <math>4 \times \left(\frac{16\pi}{3} - 4\sqrt{3}\right)</math></p> </div> </div>
<p>How much of the circle, centre B is shaded?</p>	$\begin{aligned} \text{Area of the circle - red area} &= 16\pi - 4 \left(\frac{16\pi}{3} - 4\sqrt{3}\right) \\ &= 16\pi - \frac{64\pi}{3} + 16\sqrt{3} \\ &= 16\sqrt{3} - \frac{16\pi}{3} \end{aligned}$

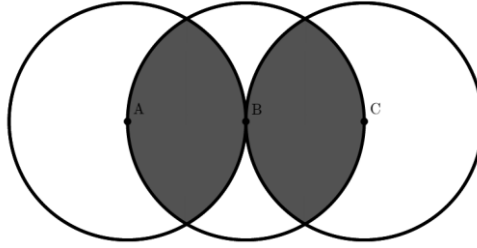
b)  
 The diagram shows three circles, each of radius 6cm.  
 The centres of the circles are A, B and C such that ABC is a straight line and  $AB = BC = 6\text{cm}$ .



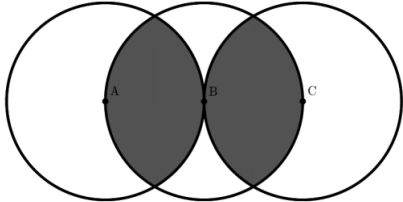
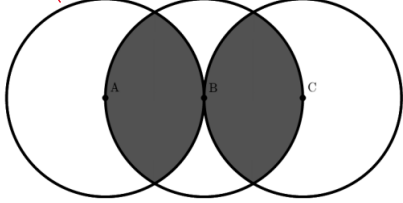
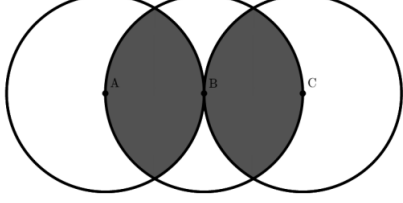
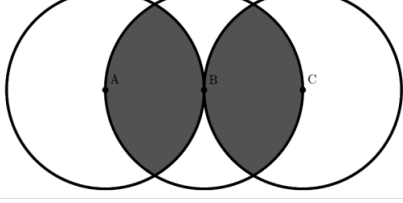
Work out the area of the shaded region.  
 Give your answer in terms of  $\pi$ .

<p>What is the area of each circle?</p>	$A = \pi r^2 = \pi \times 6^2 = 36\pi$
<p>How much of the circle, centre B, is unshaded?</p>	<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <p>A regular hexagon, formed of six equilateral triangles, is inscribed in a circle.</p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the sector = <math>\frac{1}{3} \times 36\pi = 12\pi</math></p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the triangle = <math>\frac{1}{2} \times 6 \times 6 \times \sin 120 = 18 \times \frac{\sqrt{3}}{2} = 9\sqrt{3}</math></p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the segment = Area of sector - area of triangle =</p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  </div>
<p>How much of the circle, centre B is shaded?</p>	

c)  
 The diagram shows three circles, each of radius 5cm.  
 The centres of the circles are A, B and C such that ABC is a straight line and  $AB = BC = 5\text{cm}$ .



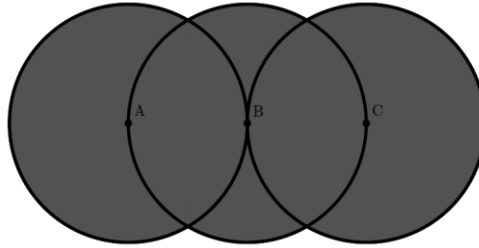
Work out the total area of the two shaded regions.  
 Give your answer in terms of  $\pi$ .

<p>What is the area of each circle?</p>	$A = \pi r^2 = \pi \times 5^2 = 25\pi$
<p>How much of the circle, centre B, is shaded?</p>	<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <p>A regular hexagon, formed of six equilateral triangles, is inscribed in a circle.</p> <p>Area of the sector =</p>    <p>Area of the triangle =</p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the triangle =</p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the triangle =</p> </div> </div> <div style="display: flex; align-items: center; margin-top: 20px;">  <div style="margin-left: 20px;"> <p>Area of the triangle =</p> </div> </div>

d)

The diagram shows three circles, each of radius 5cm.

The centres of the circles are A, B and C such that ABC is a straight line and  $AB = BC = 5\text{cm}$ .



Work out the area of the shaded region.

Give your answer in terms of  $\pi$ .