a)

A, B, C, D and E are points on a straight line.

$A, B, C$ and $D$ are equally spaced.
$\mathrm{AD}: \mathrm{DE}=2: 1$.
$A$ is the point $(5,26)$ and $B$ is the point $(11,22)$.
Work out the coordinates of the point E .

What is the vector
$\overrightarrow{A D}$ ?

$$
\begin{gathered}
\overrightarrow{A D}=3 \overrightarrow{A B} \\
\overrightarrow{A B}=\binom{11-5}{22-26}=\binom{6}{-4} \\
\overrightarrow{A D}=3 \overrightarrow{A B}=3 \times\binom{ 6}{-4}=\binom{18}{-12} \\
\mathrm{AD}: \mathrm{DE}=2: 1
\end{gathered}
$$

What is the vector

$$
\overrightarrow{D E} ?
$$

$$
\overrightarrow{D E}=\frac{1}{2} \overrightarrow{A D}=\frac{1}{2} \times\binom{ 18}{-12}=\binom{9}{-6}
$$

What are the coordinates of $D$ ?

$$
D=A+\overrightarrow{A D}=(5,26)+\binom{18}{-12}=(23,14)
$$

What are the coordinates of E ?

$$
E=D+\overrightarrow{D E}=(23,14)+\binom{9}{-6}=(32,8)
$$

b)

A, B, C, D and E are points on a straight line.

$A, B, C$ and $D$ are equally spaced.
$\mathrm{AD}: \mathrm{DE}=3: 2$.
$A$ is the point $(4,35)$ and $B$ is the point $(9,29)$.
Work out the coordinates of the point E .

What is the vector
$\overrightarrow{A D}$ ?

$$
\begin{gathered}
\overrightarrow{A D}=3 \overrightarrow{A B} \\
\overrightarrow{A B}=\binom{9-4}{29-35}=\binom{5}{-6}
\end{gathered}
$$

.

$$
0
$$

$$
\overrightarrow{A D}=3 \overrightarrow{A B}=3 \times\binom{ 5}{-6}=\binom{15}{-18}
$$

What is the vector

$$
\mathrm{AD}: \mathrm{DE}=3: 2
$$

$$
\overrightarrow{D E} ?
$$

$$
\overrightarrow{D E}=\frac{2}{3} \overrightarrow{A D}=\frac{2}{3} \times\binom{ 15}{-18}=\binom{10}{-12}
$$

What are the coordinates of D ?

What are the coordinates of E ?
c)
$\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$ and E are points on a straight line.

$A, B, C$ and $D$ are equally spaced.
$\mathrm{AC}: C E=3: 4$.
$A$ is the point $(5,40)$ and $B$ is the point $(8,34)$.
Work out the coordinates of the point E .

$$
\overrightarrow{A C}=2 \overrightarrow{A B}
$$

What is the vector
$\overrightarrow{A C}$ ?

$$
\begin{gathered}
\overrightarrow{A B}=\binom{8-5}{34-40}=\binom{3}{-6} \\
\overrightarrow{A C}=2 \overrightarrow{A B}=2 \times\binom{ 3}{-6}=\binom{6}{-12}
\end{gathered}
$$

What is the vector $\overrightarrow{C E}$ ?

What are the coordinates of C?

What are the coordinates of E ?
d)
$\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$ and E are points on a straight line.

$A, B, C$ and $D$ are equally spaced.
$\mathrm{AD}: \mathrm{DE}=3: 2$.
$A$ is the point $(4,45)$ and $B$ is the point $(8,40)$.
Work out the coordinates of the point E .

